

Properties of Exponents

An exponent (also called power or degree) tells us how many times the base will be multiplied by itself. For example x^5 , the exponent is 5 and the base is x . This means that the variable x will be multiplied by itself 5 times. You can also think of this as x to the fifth power.

Below is a list of properties of exponents:

Properties	General Form	Application	Example
Product Rule <i>Same base add exponents</i>	$a^m a^n$	a^{m+n}	$x^5 x^3 = x^{5+3} = x^8$
Quotient Rule <i>Same base subtract exponents</i>	$\frac{a^m}{a^n}$	a^{m-n}	$\frac{x^9}{x^5} = x^{9-5} = x^4$
Power Rule I <i>Power raised to a power multiply exponents.</i>	$(a^m)^n$	a^{mn}	$(x^3)^4 = x^{3 \cdot 4} = x^{12}$
Power Rule II <i>Product to power distribute to each base</i>	$(ab)^m$	$a^m a^n$	$(4x^3)^2 = 4^2 x^{3 \cdot 2} = 16x^6$
Negative Exponent I <i>Flip and change sign to positive</i>	a^{-m}	$\frac{1}{a^m}$	$x^{-3} = \frac{1}{x^3}$
Negative Exponent II <i>Flip and change sign to positive</i>	$\frac{1}{a^{-m}}$	a^m	$\frac{1}{x^{-5}} = x^5$
Zero Exponent <i>Anything to the zero power (except 0) is one</i>	a^0	$a^0 = 1$	$(-4x)^0 = 1$

- It is important to note that none of these applications can occur if the bases are not the same.

For example, $\frac{x^5}{y^3}$ cannot be simplified.